

Complexity Example *

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Sample Algorithms

- Determine **Big O** complexity for following algorithms in Python!
- Background
 - This presentation embeds `klipse`, to enable live code execution.
 - * Thus, click into code on next slides, edit it, and have results immediately displayed.
 - If code does not execute, maybe reload without cache (Ctrl+F5 in Firefox)
 - Based on in-browser implementation of Python (`skulpt`), not complete.

Instructions

1. Figure out what the algorithms on the next slides do.
 - If you are not sure, maybe copy&paste into `Python Tutor`, which enables step-by-step execution with visualizations of values.
2. Determine the algorithms' complexities in terms of numbers of necessary plus operations.
 - If you are puzzled about the focus on plus operations, note that they occur at the inner-most level of nesting in `while` loops. For each iteration of a loop, a fixed number of other operations is executed, and those are covered by a constant factor in the definition of **Big O** complexity (M at Wikipedia.)

Subsequent quizzes lead to solutions. Please try yourself first.

*This PDF document is an inferior version of an OER HTML page; free/libre Org mode source repository.

Naive Multiplication

```
def naive_mult(op1, op2):
    if op2 == 0: return 0
    result = op1
    while op2 > 1:
        result += op1
        op2 -= 1
    return result

print(naive_mult(2, 3))
```

A solution

Naive Exponentiation

```
def naive_mult(op1, op2):
    if op2 == 0: return 0
    result = op1
    while op2 > 1:
        result += op1
        op2 -= 1
    return result

def naive_exp(op1, op2):
    if op2 == 0: return 1
    result = op1
    while op2 > 1:
        result = naive_mult(result, op1)
        op2 -= 1
    return result

print(naive_exp(2, 3))
```

- Some notes
 - Code on left is meant for non-negative integers
 - * Better code would test this
 - Python basics
 - * `def naive_mult(op1, op2)` declares function `naive_mult` with two operands
 - * `==` tests for equality, `=` is assignment to variable on left
 - * `result += op1` is short for `result = result + op1`
 - thus, `op1` is added to `result`
 - `-=` similarly
 - * `return` exits the function, delivers result

- Some notes
 - `naive_mult` is copied from previous slide
 - `naive_exp` shares same basic structure
 - * But with invocation of `naive_mult` instead of plus operation

A solution

A “Small” Change

- What happens if the order of arguments to `naive_mult` on the previous slide was reversed, i.e., if `naive_mult(op1, result)` instead of `naive_mult(result, op1)` was executed?
 - Clearly, as multiplication is commutative, the result does not change.
 - What about the resulting complexity?

A surprise?

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